Welcome!
Today's Agenda:

- Ray Tracing Recap
- Shading
- Textures
Ray Tracing

World space

- Geometry
- Eye
- Screen plane
- Screen pixels
- Primary rays
- Intersections
- Point light
- Shadow rays

Light transport

- Extension rays

Light transport
Recap

Ray definition

A ray is an infinite line with a start point:

\[ p(t) = O + t\vec{D}, \text{ where } t > 0. \]

The ray direction is generally *normalized*.

Struct `Ray`

```cpp
struct Ray {
    float3 O; // ray origin
    float3 D; // ray direction
    float t;  // distance
};
```

Ray setup

Point on the screen: \( p(u, v) = p_0 + u(p_1 - p_0) + v(p_2 - p_0), \) \( u, v \in [0,1] \)

Ray direction (before normalization): \( \vec{D} = p(u, v) - E \)

\[
\vec{D} \cdot \vec{N} = \vec{D}_x \vec{N}_x + \vec{D}_y \vec{N}_y + \vec{D}_z \vec{N}_z \\
O \cdot \vec{N} = O_x \vec{N}_x + O_y \vec{N}_y + O_z \vec{N}_z
\]

\[
t = -(O \cdot \vec{N} + d) / (\vec{D} \cdot \vec{N})
\]
Today's Agenda:

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- Shading
- Textures
Shading
Shading

The End

We used *primary rays* to find the *primary intersection* point.

Determining light transport:

- Sum illumination from all light sources
- ...If they are *visible*.

We used a primary ray to find the object visible through a pixel:
Now we will use a *shadow ray* to determine visibility of a light source.
Shading

Shadow Ray

Constructing the shadow ray:

\[ p(t) = O + tD \]

Ray origin: the primary intersection point \( I \).

Ray direction: \( P_{\text{light}} - I \) (normalized)

Restrictions on \( t \): \( 0 < t < |P_{\text{light}} - I| \)
Shading

Shadow Ray

Direction of the shadow ray:

\[
\frac{P_{light} - I}{\|P_{light} - I\|}
\]

Equally valid:

\[
\frac{I - P_{light}}{\|P_{light} - I\|} \quad \text{or} \quad \frac{I - P_{light}}{\|I - P_{light}\|}
\]

Note that we get different intersection points depending on the direction of the shadow ray.

It doesn't matter: the shadow ray is used to determine if there is an occluder, not where.

This has two consequences:

1. We need a dedicated shadow ray query;
2. Shadow ray queries are (on average) twice as fast. (why?)
Shading

Shadow Ray

“In theory, theory and practice are the same. In practice, they are not.”

Problem 1:

Our shadow ray queries report intersections at $t = \sim 0$. Why?

Cause: the shadow ray sometimes finds the surface it originated from as an occluder, resulting in shadow acne.

Fix: offset the origin by ‘epsilon’ times the shadow ray direction.

Note: don’t forget to reduce $t_{max}$ by epsilon.
Shading

Shadow Ray

“In theory, theory and practice are the same. In practice, they are not.”

Problem 2:

Our shadow ray queries report intersections at $t = t_{\text{max}}$. Why?

Cause: when firing shadow rays from the light source, they may find the surface that we are trying to shade.

Fix: reduce $t_{\text{max}}$ by $2 \times \epsilon$.
Shading

Shadow Ray

“The most expensive shadow rays are those that do not find an intersection.”

Why?

(because those rays tested every primitive before concluding that there was no occlusion)
Shading

Transport

The amount of energy travelling from the light via the surface point to the eye depends on:

- The brightness of the light source
- The distance of the light source to the surface point
- Absorption at the surface point
- The angle of incidence of the light energy
Shading

Transport

Brightness of the light source:

Expressed in **watt (W)**, or **joule per second (J/s or J s\(^{-1}\))**.

Energy is transported by photons.

Photon energy depends on wavelength; energy for a ‘yellow’ photon is \(\sim 3.31 \times 10^{-19} \text{ J}\).

A 100W light bulb thus emits \(\sim 3.0 \times 10^{21} \text{ photons per second}\).
Energy at distance $r$:

For a point light, a brief pulse of light energy spreads out as a growing sphere. The energy is distributed over the surface of this sphere.

Energy per unit area is therefore proportional to the inverse area of the sphere at distance $r$, i.e.:

$$\frac{E}{m^2} = E_{\text{light}} \frac{1}{4\pi r^2}$$

Light energy thus dissipates at a rate of $\frac{1}{r^2}$.

This is referred to as distance attenuation.
Shading

Transport

Absorption:

Most materials absorb light energy. The wavelengths that are not fully absorbed define the ‘color’ of a material.

The reflected light is thus:

\[ E_{\text{reflected}} = E_{\text{incoming}} \odot C_{\text{material}} \]

Note that \( C_{\text{material}} \) cannot exceed 1; the reflected light is never more than the incoming light.

\( C_{\text{material}} \) is typically a vector: we store r, g, b for all light transport.

\[ A \odot B = \begin{bmatrix} A_x B_x \\ A_y B_y \\ A_z B_z \end{bmatrix} \text{ (‘entrywise product’)} \]
Shading

Transport

Energy arriving at an angle:

A small bundle of light arriving at a surface affects a larger area than the cross-sectional area of the bundle.

Per $m^2$, the surface thus receives less energy. The remaining energy is proportional to:

$$\cos \alpha \quad \text{or} \quad \vec{N} \cdot \vec{L}.$$
Shading

Transport

All factors:

- **Emitted light**: defined as RGB color, floating point.
- **Distance attenuation**: \( \frac{1}{r^2} \)
- **Absorption**: modulate by material color.
- **N dot L**
Shading

```c
// Shading code snippet
```

INFOGR – Lecture 5 – “Ray Tracing”
Today's Agenda:

- Ray Tracing Recap
- Shading
- Textures
Texturing a Plane

Given a plane: $y = 0$ (i.e., with a normal vector $(0,1,0)$).

Two vectors on the plane define a basis:

Using these vectors, any point on the plane can be reached:

We can now use $\lambda_1, \lambda_2$ to define a color at $P$:

$$F(\lambda_1, \lambda_2) = \cdots.$$
Textures

Example:

\[ F(\lambda_1, \lambda_2) = \sin(\lambda_1) \]

Another example:

\[ F(\lambda_1, \lambda_2) = (\text{int}(2 \times \lambda_1) + \text{int}\lambda_2) \& 1 \]
Textures

Other examples (not explained here):

Perlin noise
Details:  http://www.noisemachine.com/talk1

Voronoi / Worley noise
Textures

INFOGRAPHIC

Lecture 3

"Geometry"
Textures

Obviously, not all textures can be generated procedurally.

Finding $P$ using basis vectors $\vec{u}$, $\vec{v}$ and parameters $\lambda_1, \lambda_2$:

$$
(P_x, P_y) = \lambda_1 \vec{u} + \lambda_2 \vec{v} = 
\left( \begin{array}{c}
\lambda_1 \vec{u}_x + \lambda_2 \vec{v}_x \\
\lambda_1 \vec{u}_y + \lambda_2 \vec{v}_y 
\end{array} \right)
$$

...But what about the opposite, i.e. can we find $\lambda_1, \lambda_2$ given $P$?
Textures

Obviously, not all textures can be generated procedurally.

For the generic case, we lookup the color value in a pixel buffer.

\[
\begin{pmatrix}
\bar{x} \\
\bar{y}
\end{pmatrix} = \left( P \cdot \bar{u} \right) \cdot \left( \frac{T_{width}}{T_{height}} \right)
\]

Note that we find the pixel to read based on \( P \); we don’t find a ‘\( P \)’ for every pixel of the texture.
Textures

Retrieving a pixel from a texture:

\[
\begin{align*}
(x, y) &= \left( \frac{P \cdot \vec{u}}{P \cdot \vec{v}} \right) \times \left( \frac{T_{\text{width}}}{T_{\text{height}}} \right)
\end{align*}
\]

We don't want to read outside the texture. To prevent this, we have two options:

1. **Clamping**

\[
\begin{align*}
(x, y) &= \left( \frac{\text{clamp}(P \cdot \vec{u}, 0, 1)}{\text{clamp}(P \cdot \vec{v}, 0, 1)} \right) \times \left( \frac{T_{\text{width}}}{T_{\text{height}}} \right)
\end{align*}
\]

2. **Tiling**

\[
\begin{align*}
(x, y) &= \left( \frac{\text{frac}(P \cdot \vec{u})}{\text{frac}(P \cdot \vec{v})} \right) \times \left( \frac{T_{\text{width}}}{T_{\text{height}}} \right)
\end{align*}
\]

Tiling is efficiently achieved using a bitmask. This requires texture dimensions that are a power of 2.
Textures

Texture mapping: oversampling
Textures

Texture mapping: undersampling
Textures

Fixing oversampling

Oversampling: reading the same pixel from a texture multiple times.
Symptoms: blocky textures.

Remedy: bilinear interpolation:
Instead of clamping the pixel location to the nearest pixel, we read from four pixels.

\[
\begin{align*}
w_{p1} & : (1 - \text{frac}(x)) \times (1 - \text{frac}(y)) \\
w_{p2} & : \text{frac}(x) \times (1 - \text{frac}(y)) \\
w_{p3} & : (1 - \text{frac}(x)) \times \text{frac}(y) \\
w_{p4} & : 1 - (w_{P1} + w_{P2} + w_{P3})
\end{align*}
\]
Textures

Fixing oversampling
Textures

Fixing undersampling

Undersampling: skipping pixels while reading from a texture.
Symptoms: Moiré, flickering, noise.

Remedy: MIP-mapping.

The texture is reduced to 25% by averaging 2x2 pixels. This is repeated until a 1x1 image remains.

When undersampling occurs, we switch to the next MIP level.
Texture [INFOGR] - Lecture 3 - "Geometry"
Textures

Trilinear interpolation: blending between MIP levels.
Today’s Agenda:

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Need help?

Tuesday May 15, 13:15

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END OF lecture 5: “Ray Tracing”

Next lecture: “Ray Tracing (2)”